## Effect of Distant Scatterers on MIMO Fading Channel Tracking

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This paper considers the problem of a wireless multi-input multi-output (MIMO) fading channel tracking, when a strong distant scattering cluster is present in the area in addition to the local scattering zone around the mobile. Time-varying fading channels are dynamic in nature and their tap values in signal processing depend significantly on the distribution of the angle of arrival (AOA)  $p(\psi)$  at the mobile station. We assume  $N_T$ -input,  $N_R$ -ouput MIMO communication system where each receiver antenna observes a linear combination of all transmitted data sequences, each distorted by ISI, under white Gaussian noise [1]. Using state-space approach, a MIMO system operating over time-varying channel, can be modeled as, [1,2].

$$h_l^{(m,j)}(i+1) = \alpha_l^{(m,j)} h_l^{(m,j)}(i) + v_l^{(m,j)}(i+1)$$
(1)

$$r^{(j)}(i) = \sum_{m=1}^{N_T} \sum_{l=1}^{L^{(m,j)}} h_l^{(m,j)}(i) x^{(m)}(i-l) + n^{(j)}(i)$$
(2)

where  $h_l^{(m,j)}(i)$  is the *l*th tap of the impulse response of order  $L^{(m,j)}$  between the *m*th input  $x^{(m)}(i)$  (with  $m = 1, \ldots, N_T$ ), and the *j*th ouput  $r^{(j)}(i)$  (with  $j = 1, \ldots, N_R$ ), of the time-varying MIMO channel, at time instant *i*.  $x^{(m)}(i)$  is the transmitted signal from transmitter *m*, and  $r^{(j)}(i)$  is the received signal at receiver *j*.  $v_l^{(m,j)}(i)$  and  $n^{(j)}(i)$  are i.i.d. process and measurement noises and  $\alpha_l^{(m,j)}$  is the autoregressive (AR) coefficient of *l*th tap and accounts for the variations in the channel due to spatially dispersed multipath signals affected by the maximum Doppler shift  $f_D^{(l)}$  [1–3].

$$\alpha_l = E\{h_l(i)h_l^*(i-1)\} = \int_{-\pi}^{\pi} p(\psi)e^{-j2\pi f_D^{(l)}T\cos(\psi)}d\psi$$
(3)

where T is the symbol duration. In rural or sub-urban areas, when mobile travels at fast speed under the influence of a dominant distant scatterer (e.g., hill), the distribution of the AOA,  $p(\psi)$  deviates from the uniform shape (a common assumption usually made to find correlation statistics [1–3]), and can be written as,

$$p(\psi) = \Omega \frac{R^2 + 4D\cos(\psi - \psi_D)\sqrt{R^2 - D^2\sin^2(\psi - \psi_D)}}{\pi R^2}$$
(4)

where R is the radius of the distant scattering cluster, D is the distance of its center from the mobile,  $\psi_D$  is the angle it makes with the virtual line of sight at mobile and  $\Omega$  is the normalizing constant.

A variety of models may be used with different values of D, R and  $\psi_D$  depending on the terrain and geography of the area to obtain  $\alpha_l$ , which can then be exploited in fading channel tracking algorithms using (1) and (2).

## REFERENCES

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